# Effect of Flux Surface Shape on the Adiabaticity of Fast Ions in Spherical Tori

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# 1. Introduction

Relatively strong inhomogeneity of the magnetic field **B** of axisymmetric low-aspectratio spherical torus (ST) plasmas is known to cause non-conservation of the magnetic moment  $\mu$  of fast ions confined in these devices [1,2]. Here we evaluate non-adiabatic variations of the magnetic moment of fast ions as effected by small-scale (in poloidal angle  $\chi$ ) perturbations of the flux surface (FS) shape of high beta ST equilibria. These perturbations arise from the combined effects of plasma paramagnetism and large Shafranov shift of noncircular flux surfaces, causing  $|\mathbf{B}|=B$  to vary non-monotonically as a field line is followed from its inner to the outer mid-plane crossing point. The resulting small-scale modulation of the magnetic field we will call poloidal field (PF) ripples in analogy with the toroidal field ripples. For NSTX with  $\beta=23\%$ , Fig. 1 displays the EFIT equilibrium *B*-contours in flux coordinates (r,  $\chi$ ), where r denotes the FS radius. It can be seen that PF ripples exist at the outboard part of the plasma column (90°< $\chi$ <270° and r>0.8a,  $\chi=180°$  corresponds to the NSTX equator).

# 2. Model ST magnetic field

Our consideration is based on a model magnetic field  $B_0(\chi)$  with non-circular but poloidally smooth FSs [3]. To introduce the poloidally small-scale flux surface perturbation in accordance with the FS representation  $\{R_0(r,\chi), Z_0(r,\chi)\}$  of [3] we use  $R=R_0$  and  $Z=Z_0+\delta Z=Z_0[1-\delta(r)(1-M(r)\cos^2\chi)^2\cos\chi]$ ; here  $\delta(r)<<1$  and M(r)>1 define the magnitude and the poloidal scale of FS perturbation, respectively. At  $\delta(r)=\delta_0(r/a)^2$  and  $M(r) \approx 3$ , where  $\delta_0=\delta(a)$  and *a* is the plasma radius, the chosen FS perturbation  $\delta Z$  corresponds qualitatively to the axisymmetric perturbation  $\delta B \sim 0.01 B_0(\chi) \cos(6\chi)$  which fits the equilibrium FSs and



Fig. 1: EFIT equilibrium B contours in NSTX ( $\beta$ =23%)

 $B(\chi)$  in NSTX (with  $\beta = 40\%$ ) better than  $B_0(\chi)$ . This is demonstrated in Figs. 2, 3 where FSs and  $B(\chi)$  are displayed for a given flux surface radius r = 0.5 m for unperturbed, perturbed and EFIT magnetic fields. The main difference between  $B_0$  and the EFIT field is observed at the outboard part of the plasma column. It is seen that  $\delta Z$ with  $\delta_0=0.06$  and M=2.7 induces additional modulation of  $B_0(\chi)$  yielding reasonable agreement with the EFIT field. At the same time the model magnetic field is free of numerical

poloidal *B*-oscillations as given by EFIT. Fig. 4 displays the model *B* contours in NSTX with  $\beta$ =40%. Poloidal ripples exist in this case at poloidal angles (110°-120°) < $\chi$ <(240°-250°) and



Fig. 2: Poloidal dependenciesFig. 3:FSs of modelFig. 4: Model B contours in NSTXof model and EFIT Band EFIT B $(\beta=40\%)$  with  $\delta_0=0.06$ , M=2.7

*r*>0.75*a*. It can be seen that the poloidal scale of  $\beta$ =40% PF ripples in NSTX is about 80 to 85% of the poloidal scale of ripples in the  $\beta$ =23% case.

## 3. Effect of small-scale poloidal FS shape perturbations on nonadiabatic jumps of $\mu$

We consider first the contribution of the FS shape perturbations to the non-adiabatic variations of the magnetic moment. Fig. 5 demonstrates the time variations of the magnetic moment of 40 *keV* co-moving deuterons in NSTX ( $\beta$ =40%) for different magnitudes of FS shape perturbations ( $0 \le \delta_0 \le 0.08$ ) assuming the same initial conditions during more than 8 bounce periods, i.e.  $R_0 = 1.43$ m,  $Z_0 = Z_{mag}$  corresponding to the vertical position of magnetic axis,  $V_{\omega 0}/V = 0.62$  and the normalised magnetic moment  $\lambda_0 = \mu_0 B(r=0)/E=0.207$ . For strong



Fig. 5: Variations of  $\mu$  of 40 keV co-going deuterons in a NSTX-like B-field induced by small-scale FS perturbations.

shape perturbations ( $\delta_0 > 0.04$ ) a significant FS enhancement of the non-adiabatic variations of  $\mu$  is seen, while the effect of PF ripples associated with  $\delta_0 \leq 0.02$  is only weak.

The corresponding full gyro-orbits in the  $\{R, Z\}$ plane for  $\delta_0=0$  and  $\delta_0=0.06$  are shown in Fig. 6. According to the analytical estimations [4,1] the nonadiabatic jumps of the magnetic moment per bounce period is  $\Delta \mu \approx \Delta \mu_{\text{max}} \cos(\theta + \alpha)$ , where  $\Delta \mu_{\text{max}}$  denotes the maximum non-adiabatic variation of  $\mu$  per bounce period, is the gyro-phase when the particle has  $\theta$ crossed the mid-plane and  $\alpha$  a constant.

The numerically calculated non-adiabatic jumps of  $\mu$  are depicted in Fig. 7 as a function of  $\theta$  using the







as a function the gyro-phase when the particle has crossed the mid-plane

agreement with the analytical predictions confirming the resonant nature of the non- adiabatic jumps of  $\mu$ .

Finally we consider the contribution of the poloidal field ripples to  $\Delta \mu_{\text{max}}$ . In Fig. 8 we display the numerically obtained dependence of  $\Delta \mu_{max}$  on the magnitude of the FS shape perturbation,  $\delta_0$ , for the parameters of Fig. 5. As already mentioned, the dependence



Fig. 8: Magnitude of nonadiabatic jumps of magnetic moment vs the magnitude of FS shape perturbation

 $\Delta \mu_{\text{max}}(\delta_0)$  is essentially nonlinear. For  $\delta_0 \le 0.02$  the contribution of FP ripples is weak and  $\Delta \mu_{\text{max}}(\delta_0) \approx \Delta \mu_{\text{max}}(0)$ , whereas for  $\delta_0 > 0.02$  we obtained  $\Delta \mu_{\text{max}}(\delta_0) \sim \delta_0^{2}$ . For  $\delta_0 = 0.06$  corresponding to the EFIT poloidal modulation of  $B_0$ , and for a flux surface radius r = 0.445m = 0.7a, the PF ripples enhance the non-adiabatic changes of the magnetic moment of 40 *keV* deuterons by more than 10 times. The effect considered is expected to play an important role in the confinement and transport of fast ions in spherical tori.

# 4. Summary

The present investigation demonstrates the substantial effect of small-scale poloidal perturbations of the flux surface shape on the non-adiabaticity of fast ions in spherical tori. In high beta ST plasmas, almost all non-adiabatic variations of the magnetic moment of fast ions are induced by poloidal field ripples. PF ripple induced relative jumps of the magnetic moment,  $\Delta \mu_{\text{max}} / \mu_0$ , of 40 *keV* deuterons in NSTX are of the order of 10-20% at the plasma periphery (*r*/*a*>0.7). The new PF-ripple effect is expected to play an important role in the confinement and transport of fast ions in spherical tori as well as in stellarators.

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