

# 'Complete' far-infrared polarimetry measurements at JET

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## 1. Introduction

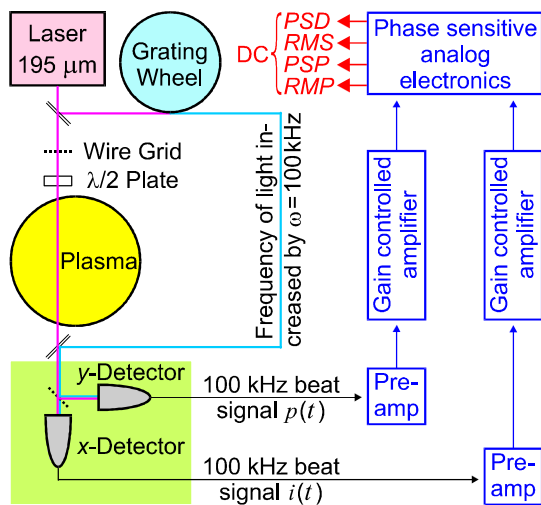
Far-infrared polarimetry is a well known tool to measure the poloidal field  $B_p$  in terms of the density-weighted line-of-sight integral of  $B_{p||}$  which is proportional to the Faraday rotation angle of the plane of polarization. This 'traditional' polarimetry provides important data to calculate the  $q$ -profile, but does not exploit the method completely: The output ellipticity of the beam, generated by the Cotton-Mouton effect (birefringence of a magnetized plasma), carries line-integrated information on density and magnetic field components perpendicular to the direction of the beam. This concerns  $B_t$  in good approximation – the toroidal field  $B_t$  alone, which is, in the case of vertical chords, largely constant along the line of sight. Hence, complete polarimetry can additionally deliver the line-integrated density [1], which is otherwise measured routinely by interferometry with the drawback of fringe jumps [2].

It is the phase shift  $\Phi'$  between the wave components parallel and perpendicular to  $B_t$  which is proportional to  $\int n_e dz$  (vertical chord!). Its measurement requires the input polarization to be different from parallel or perpendicular ( $\Theta' = 0$  or  $90^\circ$ ), contrary to the customary approach. The latter aims to suppress the Cotton-Mouton effect as much as possible in order to obtain the rotation angle in a most simple way and get around the obstacle of spurious ellipticity generated in the optical system. Complete polarimetry, however, needs to tackle this serious problem, and the way it has been solved at JET is a major topic of this paper.

Another issue where novel results are presented is the mutual interference of Faraday and Cotton-Mouton effects: The former changes the phase shift, too, and the latter has an impact on the polarization angle. The pertinent theory that allows a approximate reconstruction of the 'pure' effects is given in [3]; its crucial test on experimental data is subject of Section 5.

## 2. Experimental set-up

The instrument at JET comprises four vertical and four lateral channels (chords) with the same probing beams utilized for interferometry as well. The schematic in Fig. 1



**Fig. 1.** Polarimetry set-up at JET. The half-wave plate at the entrance window is used to set the required direction of the linear input polarization and, by being rotated, provides a calibration measurement before each discharge. The amplitudes of the beat signals are proportional to the corresponding electric field vector amplitudes of the electromagnetic wave in the local co-ordinate system defined by the orientation of the wire grid in front of the detectors:

$$i(t) \propto E_x^{(0)} \cos(\omega t) \text{ and } p(t) \propto E_y^{(0)} \cos(\omega t - \varphi).$$

The electronic evaluates these signals by analog multiplication and integration (2, 5, 10 ms settable) according to

$$PSD = \langle p(t) \times i(t) \rangle \quad RMS = \langle i(t) \times i(t) \rangle$$

$$PSP = \langle p(t) \times i'(t) \rangle \quad RMP = \langle i'(t) \times i'(t) \rangle$$

where  $i'(t) \propto E_x^{(0)} \sin(\omega t)$  is generated by phasing  $i(t)$ .

shows the essential experimental details for one channel. The four DC output signals, recorded with 14 ms resolution, are processed numerically to produce the following basic signals:

$$R = PSD/RMS = C^{-1} \tan\Theta \cos\phi \quad R' = PSP/\sqrt{RMS \cdot RMP} = C^{-1} \tan\Theta \sin\phi, \quad (1)$$

where the amplitude ratio angle  $\Theta$  is defined by  $\tan\Theta = E_y^{(0)}/E_x^{(0)}$  and the phase shift angle  $\phi$  includes a constant offset  $\phi_0$  due to grating-beam ellipticity, electronics, etc.:  $\phi = \Phi + \phi_0$ .

In the calibration measurement with linearly polarized light ( $\lambda/2$  plate!), i.e.  $\Phi = 0$ ,  $\phi$  should be constant and the varied input polarization angle  $\Theta'$  should figure in Eqs (1) save for an unknown offset:  $\Theta = \Theta' + \Theta_0$ . Thus, it should be straightforward to find the three calibration parameters  $\phi_0$ ,  $\Theta_0$  and  $C$ . Not so in reality!  $\phi$  varies along with  $\Theta'$  as the experimental functions  $R(\Theta')$  and  $R'(\Theta')$  have no common zeros, indicating *spurious ellipticity*.

### 3. A model to account for and eliminate spurious ellipticity

There are several ways to try and explain the origin of spurious ellipticity. Some were put to the test quantitatively (accuracy of fit of calibration data) and had to be rejected, including the assumption of an imperfect half-wave plate. The one that works consists in a model which assumes that an optical element (window, recombination plate?) generates a *constant* phase shift  $\tilde{\phi}$  that refers to a *rotated* co-ordinate system of unknown orientation  $\Xi$ .

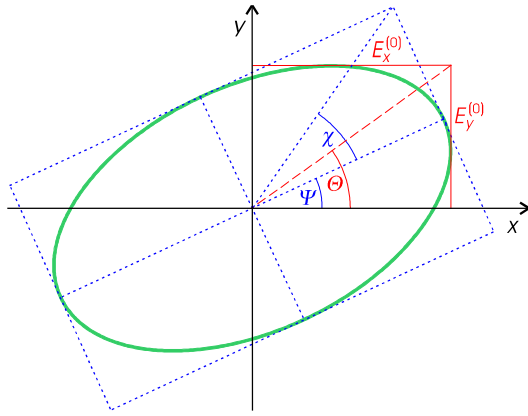


Fig. 2. Definition of parameters that describe the polarization state of elliptically polarized light.

Figure 2 shows the geometrical parameters  $\Psi$  and  $\chi$  (polarization angle  $\Psi$  and ellipticity  $\varepsilon = \tan\chi$ ) which describe the polarization state of light as completely as the characteristics of the electric field vector, i.e. amplitude ratio  $\tan\Theta$  and phase shift angle  $\Phi$ . The transformation between these two representations is given by (see [3], [4])

$$\cos 2\Theta = \cos 2\chi \cos 2\Psi \quad (2)$$

$$\tan \Phi = \tan 2\chi / \sin 2\Psi \quad (3)$$

$$\tan 2\Psi = \tan 2\Theta \cos \Phi \quad (4)$$

$$\sin 2\chi = \sin 2\Theta \sin \Phi. \quad (5)$$

These relations, valid in any co-ordinate system, are essential to evaluate the model as shown

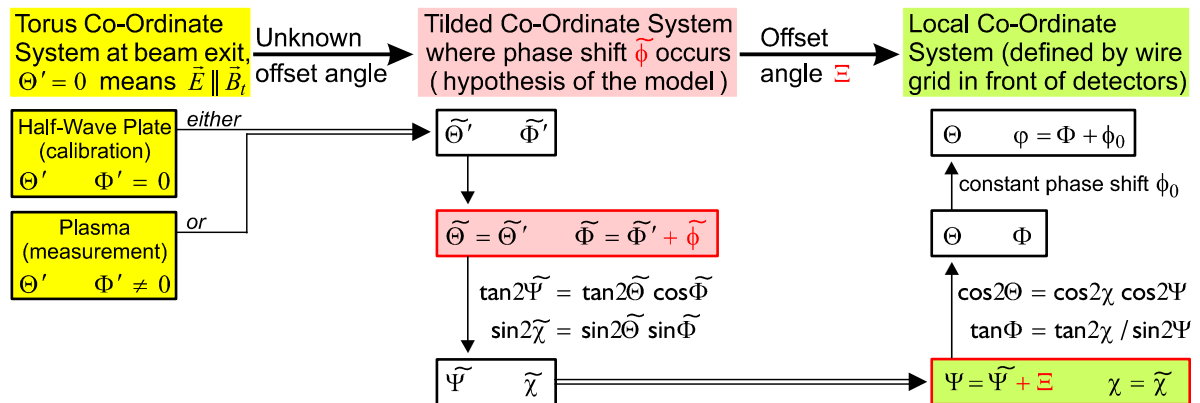


Fig. 3. Model of the origin of spurious ellipticity with unknown parameters  $\tilde{\phi}$  and  $\Xi$ .

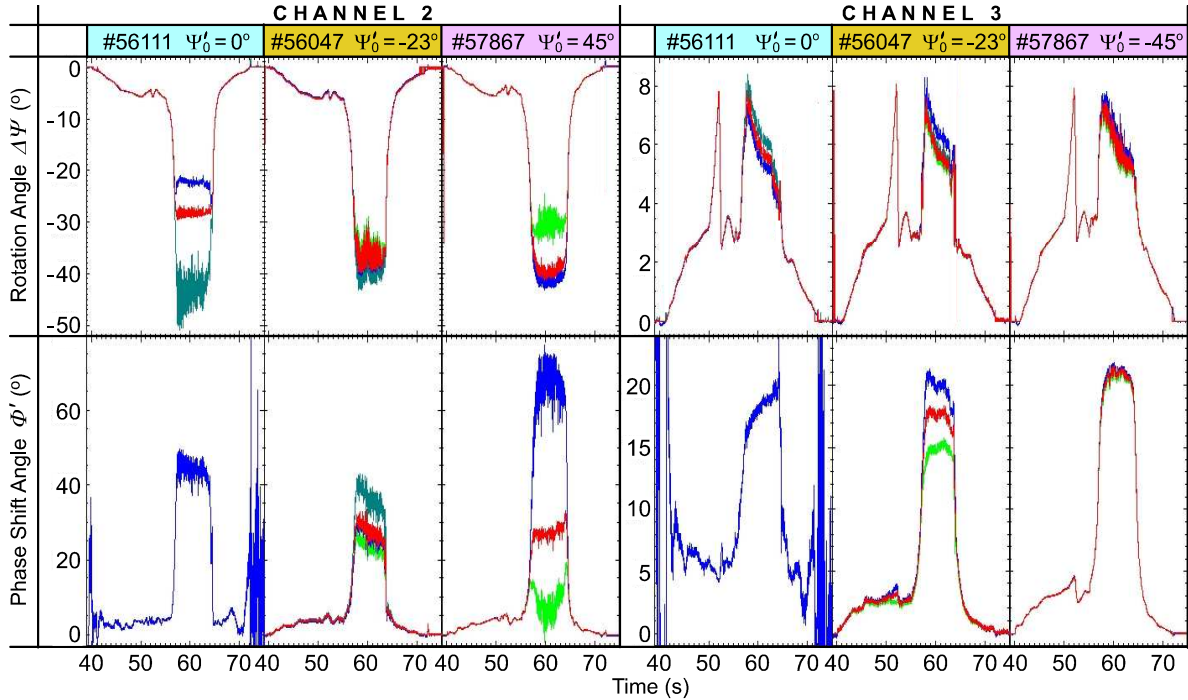
in Fig. 3. Although the model has two unknown parameters, its evaluation yields only one,  $\sin 2\xi = \sin 2\xi \sin \tilde{\phi}$ ,

apart from two other new parameters,  $\phi$  and  $\Theta'_0$ , which, however, incorporate the old ones,

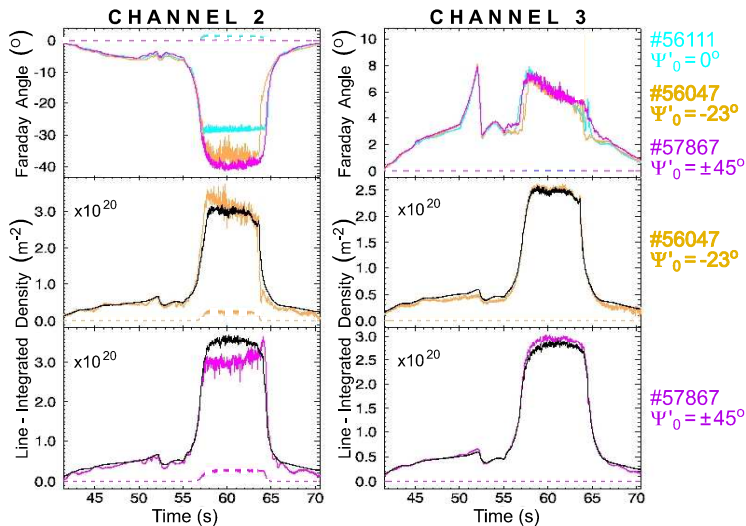


## 5. Mutual interference of Faraday effect and Cotton-Mouton effect

This phenomenon, though theoretically evident [3] and well known, has so far been disregarded in practice. Rightly so for small plasmas and the standard set-up  $\Psi'_0 = \Theta'(0) = 0$ . High-density plasmas in the large JET device, however, can produce rotation angles and phase shift angles which have little to do with the Faraday and Cotton-Mouton ones, respectively. This can be demonstrated by comparing polarimetry results obtained on very similar



**Fig. 6.** Results from similar shots ( $B_t = 2.7$  T,  $I_p = 2.5$  MA): Blue traces as measured. Red lines show the so-called ‘model mean values’, green lines the limits, both calculated, according to [3], from the experimental data.



**Fig. 7.** Comparison of ‘model means’ and their uncertainties (dotted).

discharges, using *different*  $\Psi'_0$ s.

Fig. 6 shows a suitable triplet of shots with the red lines to demonstrate the capability of the method [3] to recover the ‘pure’ quantities expected to be broadly equal.

The latter alone are re-plotted in Fig. 7 to visualize the equality – except for Channel 2 of #56111 – of the pure Faraday angles and the relevance of the Cotton-Mouton angle expressed as line-integrated densities according to Eq (9) – black lines show the interferometric  $\int n_e dz$ .

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