JET Experiments to Assess Finite Larmor Radius Effects on Resonant Ion Energy Distribution during ICRF Heating

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ABSTRACT This work reports on experimental verification of the importance of finite Larmor radius (FLR) effects on the detailed shape of the resonant ion distribution on JET tokamak during ion cyclotron resonance heating (ICRH). It is seen that not taking the FLR effects into account leads to an incorrect local ion temperature prediction. Ion energy distributions are simulated by fully including FLR effects and good agreement with neutral particle analyser (NPA) measurements has been found.

INTRODUCTION The experiments reported here continue an earlier work [1] where it was found that due to finite Larmor radius effects the wave-particle interaction at certain energies E* becomes strongly reduced, effectively preventing resonating ions from reaching higher energies. This was an important result because it showed that the FLR effects can influence the distribution function of the resonating ions, and thus they can also play a role for the absorption strength. In practise, these effects are mainly of importance for second or higher harmonic ICRF heating scenarios where E* is rather small, typically around 1 MeV in JET. One of the principal ICRF heating schemes foreseen for ITER is the second harmonic heating of tritium \( \omega = 2\omega_{\text{CT}} \). It is therefore of interest to assess the significance of FLR effects in a second harmonic heating scheme not only for physics interest but also to see whether it has implications on ITER.
RELEVANT ICRH THEORY It is possible to obtain a rough analytical estimate for the perpendicular (to the magnetic field) ion distribution \( f_{\perp} \) by solving a simplified Fokker-Planck equation for test particles as in Ref. 2

\[
\frac{\partial f(v_{\perp},t)}{\partial t} \approx - \frac{1}{v_{\perp}} \frac{\partial}{\partial v_{\perp}} \left( \alpha v_{\perp} f \right) + \frac{1}{2v_{\perp}^{2}} \frac{\partial^{2}}{\partial v_{\perp}^{2}} \left( \beta v_{\perp} f \right) + \frac{1}{4v_{\perp}^{3}} \frac{\partial}{\partial v_{\perp}} \left( \gamma f \right) + \frac{1}{v_{\perp}} \frac{\partial}{\partial v_{\perp}} \left( D_{RF} v_{\perp} \frac{\partial f}{\partial v_{\perp}} \right),
\]

where \( \alpha, \beta \) and \( \gamma \) are the Spitzer collision coefficients and \( D_{RF} \) is the RF diffusion coefficient. Here \( D_{RF} \propto |E_{+} J_{n=1}(k_{\perp} v_{\perp} / \omega_{ci}) + E_{-} J_{n=1}(k_{\perp} v_{\perp} / \omega_{ci})|^{2} \) is the full RF diffusion coefficient and not expansion as in Ref. 2. Integrating twice yields

\[
f(v_{\perp}) \approx f_{0} \exp\left(-\int_{0}^{v_{\perp}} \frac{4\alpha v_{\perp}}{2\beta v_{\perp} + 4D_{RF} v_{\perp}} \, dv_{\perp} + 2(\beta v_{\perp})' + \gamma \right).
\]

In the integrand, for reasonably high power levels, say, \( P_{ICRH} > 0.5 \text{ MW at JET}, D_{RF} \) at high energies is large compared to the other terms for a large range of plasma parameters, except close to one of its minima. \( D_{RF} \) will thus dominate the main features of the distribution. Figure 1 shows an example of the relation between the distribution and \( D_{RF} \). Note that \( E^{*} \) is also a function of electron density through the coupling between the density and \( k_{\perp} \) and that the distribution is flat when \( D_{RF} \) is large and drops rapidly when \( D_{RF} \) is small. This is markedly different from the exponential solution for \( f_{\perp} \) with the familiar effective tail temperature \( T_{eff} \propto p_{\perp} T_{e}^{3/2} / n_{r} n_{e} \) obtained by approximating \( D_{RF} \) with an effective constant value (thus ignoring the finite Larmor radius effects) and using approximate Spitzer coefficients as in Ref. 2. Here \( p_{\perp} \) is the power density absorbed by resonant species and \( n_{r} \) is their density, \( T_{e} \) is electron temperature and \( n_{e} \) is electron density.

EXPERIMENT Figure 2 shows ICRH power, neural beam power (NBI), electron density and temperature at magnetic axis and plasma diamagnetic energy for three discharges 58734, 58738 and 58739. Short duration NBI pulses at 64.1s and at 67.1s were used for diagnosing ion density and
The discharges are such that both high density pulse 58734 and high power per particle pulse 58739 are to be compared against the reference pulse 58738. Table 1 summarises the most relevant differences and similarities for these comparisons.

Table 1

<table>
<thead>
<tr>
<th>Pulse</th>
<th>$n_e(0)$</th>
<th>$P_H$</th>
<th>$T_{e0}$</th>
<th>$n_{i0}$</th>
<th>$T_{eff}$</th>
<th>$E^*$</th>
</tr>
</thead>
<tbody>
<tr>
<td>58734</td>
<td>1.5</td>
<td>1.2</td>
<td>1.0</td>
<td>0.9</td>
<td>0.9</td>
<td>0.7</td>
</tr>
<tr>
<td>58738</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>58739</td>
<td>1.0</td>
<td>1.2</td>
<td>1.7</td>
<td>1.0</td>
<td>2.4</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Temperature. The discharges are such that both high density pulse 58734 and high power per particle pulse 58739 are to be compared against the reference pulse 58738. Table 1 summarises the most relevant differences and similarities for these comparisons.

MEASUREMENTS Line integrated perpendicular energy distribution deduced from NPA [3] measurements for the three pulses (58738 appearing in two plots) are presented in Fig. 3. In the left frame one sees that the energy distribution of the high density (high $k_A$) pulse 58734 drops much more rapidly than that of the low density (low $k_A$) one 58738. This is exactly as predicted by theory. Additionally, it shows that local ion temperature for 2nd (or higher) harmonic ICRF heated ions can not be estimated with $T_{eff}$ (see Table 1) giving further evidence for the presence of FLR effects. Moreover, the frame on the right hand side shows a comparison between pulses of equal electron density (equal $k_A$). Measured distributions again follow the theory and are similar in shape. $T_{eff}$, being related to fast ion energy content, sees the difference in energy content but again fails to correctly estimate the local temperature. These complementary comparisons confirm that the resonant particles in the plasma indeed see the details of the RF diffusion operator and are blocked from reaching higher energies due to the weak wave-particle interaction close to energy $E^*$.

MODELLING Modelling of the resonant particle distribution has been made with a combination of a simplified ICRH power deposition code PION [4] and a 3-D Monte Carlo code FIDO [5] which was used to solve the 3-D Fokker-Planck equation for the distribution function. PION provided the information of the amount of power absorbed by hydrogen and the wave polarisation as well as $k_A$-spectrum for FIDO. The energy distributions calculated with this method are presented in Fig. 4 together with the experimental distributions.
DISCUSSION Although simulations agree rather well with measurements there are some effects that are not taken into account in simulations but which might have minor effects and are thus discussed briefly. The ratio between sawteeth period and ion slowing down time was roughly equal to unity for each of the discharges. Sawteeth period is considered to be long enough for the distribution to extend into its full length over time and they are thus not considered to be of importance. Electric field amplitude is taken to be constant in FIDO which is not exactly correct and could lead to a small error. Ion adiabatic motion [6] is enhanced when the wave-particle interaction is weak as it is close to $E^*$, the resonance energy. It could augment the suppression of $D_{RF}$ and therefore further reduce the formation of the high energy tail. This was verified with STOCH [7] code for one mode number and one frequency. Although STOCH predicts significant adiabaticity close to $E^*$ it is clear that it would be much reduced when including the whole spectrum and multiple frequencies. Finally, the combination of uncertainties in temperature, ion density as well as parallel and perpendicular wave spectrum can lead to an increased total error.

CONCLUSION The experimental results backed with modelling have shown that FLR effects are responsible for the lack of particles beyond critical energy $E^*$. This phenomenon gives one an opportunity to tailor the distribution to some extent. Increasing electron density will increase perpendicular wave number and therefore reduce $E^*$. Reduction of $E^*$ can also be achieved by decreasing magnetic and keeping the resonance position fixed. Due to the stronger magnetic field in ITER and future power plants $E^*$ will typically be higher than it was here. For standard ITER parameters [8] of $n_D = n_T = 5 \cdot 10^{19} \text{ m}^{-3}$, $B_T = 5.7 \text{ T}$, $f = 2f_c$, $k_A = 52 \text{ m}^{-1}$ and $E_E/E_P = 5$ we get $E^* = 7.5 \text{ MeV}$.

REFERENCES